

## Transformational Plane geometry – Errata List

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- p. 53, Proof. Let  $\rho_{C,\Theta}$  be a rotation. Let  $P$  and  $Q$  be distinct points; ...
- p. 59, #13. Let  $P = \begin{bmatrix} a \\ b \end{bmatrix}$  and  $Q = \begin{bmatrix} c \\ d \end{bmatrix}$  be points.
- p. 68, #8. ...points on  $l$  and  $l'$ , respectively, that are ... Let  $S$  and  $T$  be the feet of the perpendiculars from  $P$  and  $R$  to  $m$ , respectively.
- p. 75, Definition 137. Given intersecting lines  $l$  and  $m$ , let...
- p. 75, Section 5.2, para 2. In fact, *twice the measures of any two angles from  $l$  to  $m$  are congruent (mod 360)*.
- p. 75, Exploratory Activity 4, item 1. Construct four points, no three of which are collinear, label ...
- p. 76, Theorem 138. Given intersecting lines ...
- p. 77, Theorem 139. ...is the composition of two reflections in intersecting lines.
- p. 81, Exploratory Activity 5, item 1. Construct four points, no three of which are collinear, label ...
- p. 91, Proof. ... So assume  $A \neq B$ . Since  $\Theta + \Phi \in 0^\circ$ , either both  $\Theta$  and  $\Phi$  are multiples of 360 or neither  $\Theta$  nor  $\Phi$  is a multiple of 360. If  $\Theta, \Phi \in 0^\circ$ , then  $\rho_{A,\Theta} = \rho_{B,\Phi} = \iota$  so that  $\rho_{B,\Phi} \circ \rho_{A,\Theta} = \iota = \tau_0$  (the trivial translation). If  $\Theta, \Phi \notin 0^\circ$ , let  $\Theta' = \Theta^\circ \cap (0, 360)$ , let  $\Phi' = \Phi^\circ \cap (0, 360)$ , and let  $m = \overleftrightarrow{AB}$ . By Corollary 142, there exist unique lines  $l$  and  $n$  passing through  $A$  and  $B$ , respectively, such that  $\rho_{B,\Phi} = \sigma_n \circ \sigma_m$  and  $\rho_{A,\Theta} = \sigma_m \circ \sigma_l$ . ...
- p. 94, #8. ... let  $\tau_v = \rho_{B,120} \circ \rho_{A,240}$ , and let  $m = \overleftrightarrow{AB}$ . Use a MIRA ...
- p. 96, line 1. Then  $\sigma_m \circ \sigma_l = \rho_{C,\Theta}$  is a rotation ...
- p. 96, line 2.  $\alpha = \sigma_n \circ \rho_{C,\Theta}$  so that  $\sigma_n = \alpha \circ \rho_{C,-\Theta}$ .
- p. 107, Proof, line 2. ...let  $\alpha$  be an isometry fixing  $P$  and  $Q$ . Then  $\alpha$  fixes  $m$  pointwise. Let  $R$  be ...
- p. 107, Proof, line 6. Delete the redundant phrase " $P$ ,  $Q$ , and  $R$  are non-collinear and"
- p. 136, Proof (c), line 3. Let  $\rho_\Phi \in E$  be ...

- p. 136, Proof (c), line 8.  $\rho_\Phi = \rho_{k\Theta} = \rho_\Theta^k$ .
- p. 136, Proof (d), line 1. ...all reflections in  $G$  and let  $\sigma \in F$ . The elements ...
- p. 137, Proof of closure, line 3.  $\alpha(\beta(F)) = \alpha(F) = F$ , we have  $\alpha \circ \beta \in \text{Sym}(F)$ .
- p. 142, Example 228. Case 2:  $c$  cuts  $m$ .
- p. 146, Proof, line 4. center by Theorem 213, so this is a contradiction.
- p. 160, line -1.  $Q_1$  is not an  $n$ -center closest...
- p. 161, para 5, line 3. The points in a primitive translation lattice are vertices of parallelograms with no interior lattice points. The letter  $c$  stands for *centered lattice*, in which some non-primitive cell and its centroid form the basic building block of the tessellation.
- p. 171, lines 1 and 2. Delete the redundant sentences "Note that if  $D = \xi_{C,r}(C)$ , then  $CD = rCC = 0$  and  $D = C$ . Thus a stretch fixes its center."
- p. 172, #7. Delete the word "distinct".
- p. 187, para 3, line 1. Delete " $\beta =$ "
- p. 190, #6. ... If  $\alpha$  is a similarity,  $c$  is a line, and  $\mathbf{v}$  is...
- p. 203 line 2.  $D_5 \quad D_9 \quad D_5$

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