

p. 833 (10.5)

Find (a) the parametric equations and (b) the symmetric equations of the line.

5. The line through $(1, 2, -3)$ and parallel to $\langle 2, -1, 4 \rangle$

7. The line through $(2, 1, 3)$ and $(4, 0, 4)$

9. The line through $(1, 4, 1)$ and parallel to the line $x = 2 - 3t$, $y = 4$, $z = 6 + t$

11. The line through $(3, 1, -1)$ and parallel to the line $\frac{x-2}{3} = \frac{y+1}{-4} = \frac{z}{2}$

13. The line through $(2, 0, 1)$ and perpendicular to both $\langle 1, 0, 2 \rangle$ and $\langle 0, 2, 1 \rangle$

15. The line through $(1, 2, -1)$ and normal to the plane $2x - y + 3z = 12$

State if the lines are parallel or perpendicular or find the angle between the lines.

17. $\begin{cases} x = 1 - 3t \\ y = 2 + 4t \\ z = -6 + t \end{cases}$ and $\begin{cases} x = 1 + 2s \\ y = 2 - 2s \\ z = -6 + s \end{cases}$

19. $\begin{cases} x = 1 + 2t \\ y = 3 \\ z = -1 + t \end{cases}$ and $\begin{cases} x = 2 - s \\ y = 10 + 5s \\ z = 3 + 2s \end{cases}$

Determine if the lines are parallel, skew or intersect.

23. $\begin{cases} x = 4 + t \\ y = 2 \\ z = 3 + 2t \end{cases}$ and $\begin{cases} x = 2 + 2s \\ y = 2s \\ z = -1 + 4s \end{cases}$

25. $\begin{cases} x = 1 + 2t \\ y = 3 \\ z = -1 - 4t \end{cases}$ and $\begin{cases} x = 2 - s \\ y = 2 \\ z = 3 + 2s \end{cases}$

Find an equation of the given plane.

27. The plane containing the point $(1, 3, 2)$ with normal vector $\langle 2, -1, 5 \rangle$

29. The plane containing the point $(-2, 1, 0)$ with normal vector $\langle -3, 0, 2 \rangle$

31. The plane containing points $(2, 0, 3)$, $(1, 1, 0)$ and $(3, 2, -1)$

33. The plane containing points $(-2, 2, 0)$, $(-2, 3, 2)$ and $(1, 2, 2)$

35. The plane containing the point $(2, 1, -1)$ and parallel to the plane $3x - y + 2z = 1$

37. The plane containing the point $(0, -2, -1)$ and parallel to the plane $-2x + 4y = 3$

Sketch the given plane.

41. $x + y + z = 4$

43. $3x + 6y - z = 6$

Find the intersection of the planes.

53. $2x - y - z = 4$ and $3x - 2y + z = 0$

55. $3x + 4y = 1$ and $x + y - z = 3$

Find the distance between the given objects.

57. The point $(2, 0, 1)$ and the plane $2x - y + 2z = 4$

61. The planes $2x - y - z = 1$ and $2x - y - z = 4$

67. Suppose two airplanes fly paths described by the parametric equations

$$P_1 : \begin{cases} x = 3 \\ y = 6 - 2t \\ z = 3t + 1 \end{cases} \text{ and } P_2 : \begin{cases} x = 1 + 2s \\ y = 3 + s \\ z = 2 + 2s \end{cases} . \text{ Describe the shape of the flight paths. Determine}$$

whether the paths intersect. Determine if the planes collide.